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COUPLED AND UNCOUPLED APPROACHES FOR THIN COLD ROLLED STRIP BUCKLING PREDICTION

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ABSTRACT: Severe thin strip cold rolling conditions usually induce heterogeneity of in-bite plastic deformation always translated to irregular stress field. This stress field may dwell sufficiently compressive in several out-of-bite areas to cause buckling (flatness defects) which generates stress reorganisation in rolled strip and probably affects the bite zone. Hence, out-of-bite buckling, in-bite elastic-(visco)plastic deformation and thermo-mechanical roll-stack/strip interaction may be strongly coupled. However, a completely coupled model providing realistic rolled strip shape specially when flatness defects occur is not easy to establish. This call for two ways of flatness defect modelling in thin strip rolling: with a completely coupled approach but using a simple buckling criterion, or using an uncoupled approach by chaining strip rolling model calculation with shell element models presenting good buckling computing capabilities. Our objective is the improvement of the flat product rolling – specialized FEM software Lam3/Tec3 [1] using Counhaye simple buckling criterion [3] and Asymptotic Numerical Method (ANM) for shell element model [9,10] respectively with coupled and uncouple approaches detailed in the present paper. These two approaches bring computed stress profiles to very good agreement with experiments and the most important result at this stage is the weak influence of buckling on in-bite stress and strain fields providing a more rigorous justification of the traditional decoupled methods [2,5-8].

KEYWORDS: rolling, finite element method, flatness defect, Buckling, asymptotic numerical method.

1 INTRODUCTION

Due to severe loading in cold rolling, roll stack deformation (flattening, elastic deflection, thermal crown) induces heterogeneous elongation across strip at bite outgoing. This heterogeneity generates residual stress and buckling, named flatness defect in this context. The latter is a major industrial concern in rolling as it is one main factor for quality product.

In addition, buckling implies stress reorganization, because stresses always saturate in buckled areas. This complete rearrangement of the stress field in the post-bite strip can be considered as a change in the boundary conditions of the plastic deformation in the bite. Hence, in-the-bite and out-of-bite stress fields may be strongly coupled.

Thus, mechanical problem includes coupling combining elastic roll stack deformation, strip elastic-(visco) plastic deformation and out of bite buckling. However, most authors [2,5-8] neglect bite/post-bite coupling excepting [3].

2 THIN COLD ROLLED STRIP BUCKLING PREDICTION

2.1 COUPLED APPROACH

In a previous presentation [4], we introduced in Lam3/Tec3 [1], 3D finite element model adapted for rolling simulation, the Euler-type simple coupled buckling model criterion [3]. Since compressive stress generally saturates around a threshold value when buckling occurs in structure, it consists of an out of bite stress-relaxation algorithm. In fact, it is supposed that buckling will shorten a material element by λ wherever compressive stress exceeds σ_c . This decreases the strain sent back after each Newton-Raphson iteration to the constitutive model solver, and therefore the compressive stresses (and as a consequence, the stresses in the tensile area, to maintain mechanical equilibrium). This tends to force iteratively the stress field to respect the buckling criterion (1).

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$$\begin{cases} \sigma_c = -\frac{\pi E h^2}{3\delta^2} \\ \lambda_i = \frac{\sigma_i - \sigma_c}{k \times E} & \text{if } |\sigma_i| \geq |\sigma_c| ; \quad (i=1,2) \\ \lambda_i = 0 & \text{if } |\sigma_i| < |\sigma_c| \end{cases} \quad (1)$$

E is Young's modulus, k is a parameter representing the ratio between the material "buckling stiffness" and the Young modulus, h the strip thickness, and δ the wavelength (assumed similar to the compressive stress area dimensions). λ_I and λ_{II} are the λ components in the strip plane deduced respectively from σ_I and σ_{II} . These latter correspond to principal stresses expressed along the first and the second principal direction I and II which are defined by α angle in the laboratory reference frame.

Note that, due to the steady state nature of the model, opposed to the non-steady state character of the waves, only the occurrence of waves can be predicted with a certain degree of certainty, not their severity. Furthermore, although buckling does not occur at element scale, here it is treated locally on each element reaching the critical stress estimated in (1).

However, despite the simplicity and questionable assumptions of this model, figures 1 and 2 show, for particular rolling conditions (Table 1 : named "case 1"), that :

1. in this case (manifested flatness defect), neglecting the occurrence and effects of buckling results in a completely wrong stress profile;
2. the impact of buckling on the final stress state is to bring it much closer to experiments (measured with tensiometer roll).
3. Furthermore, we note an insignificant dependence of results on the more or less arbitrarily chosen σ_c value. This supports the criterion (1) in spite of its approximations.
4. we noted that taking account or not of buckling and its stress relaxation effect doesn't affect in-bite zone.
5. manifested flatness defects are identified as shown in figure 3, the wavy edge is visible, $\lambda_I > 0$ and angle $\alpha \approx 0^\circ$ near the edge ($I = x$); the significant λ_{II} value at the corner of the bite exit might denote a tendency to have a superimposed oblique wave ($\alpha \approx 30^\circ$). However, this simple model is unable to predict neither buckling mode nor post-buckling strip state.

2.2 UNCOUPLED APPROACH

Lam3/Tec3 coupled with a complete shell element buckling model seems certainly more relevant. However, it is very difficult to implement, and the absence of bite/buckling interaction (cf. [4]) justifies uncoupled ("chained") technique described as follows :

- At first, rolling calculation is made using Lam3/Tec3 without buckling (using a horizontal symmetry plane) providing stress distributions as well as out-of-bite stress field.

- This stress field is used as residual stress by a code based on asymptotic numerical method (ANM) [9,10] and shell element formulation for buckling plates caused by residual stresses to supply critical load, buckling mode and post-buckling state together with the new (and real) stresses distribution in strip.

Table 1: Simulated rolling operation description (case1).

Friction law	Coulomb : $\mu = 0.033$
Width	851 mm
Entry thickness	0.355 mm
Looked thickness for	0.225 mm
Upstream imposed tension	170 MPa
Incoming strip crown	2.54 %
Grinding crown	0,01614 %
Downstream imposed tension	100 MPa
Rolling velocity	22 m.s-1
Work roll diameter	555 mm
Behaviour law	Young's modulus $E = 210$ GPa Poisson's ratio $\nu = 0.3$ $\sigma_0 = (470.5 + 175.4 \times \bar{\epsilon}) \times (1 - 0.45 \times e^{-8.9\bar{\epsilon}}) - 175$, [σ_0] = (MPa)

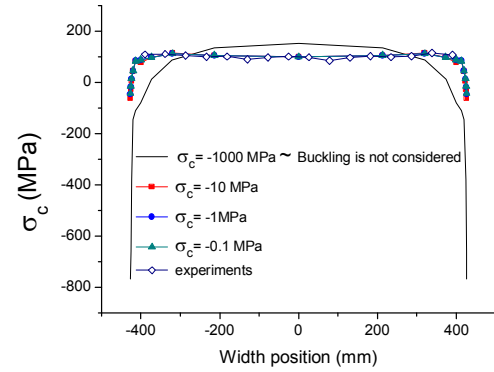


Figure 1: Comparison of stress profiles computed with and without accounting buckling, and measured in experiments (far away enough from the bite).

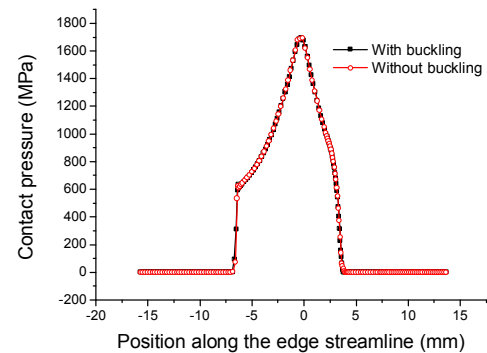


Figure 2: Work roll/Strip contact pressure profile is not influenced by buckling: on edges.

2.2.1 Asymptotic numerical method formulation

Considering Hu-Washizu functional, the stationary condition can be written in the following form

$$\phi_{\text{HW}} = \int_v \left\{ {}^t\delta S : [(\gamma_u + \tilde{\gamma}) - D^{-1} : S] + {}^tS : [\delta\gamma_u + \delta\tilde{\gamma}] \right\} dv - gP_e(\delta u) \quad (2)$$

where D is the elastic stiffness tensor, S is the second Piola Kirchhoff stress tensor, γ_u is the compatible Green Lagrange strain obtained from the displacement field and which can be decomposed into a linear and a quadratic part $\gamma_u = \gamma_l(u) + \gamma_{nl}(u, u)$. $\tilde{\gamma}$ is the enhanced part of the strain independent of the displacement and assumed to be orthogonal to the stress field. $P_e(\delta u)$ is the virtual work of external load and g is a scalar load parameter. The latter gets critical value g_c at bifurcation point when buckling happens.

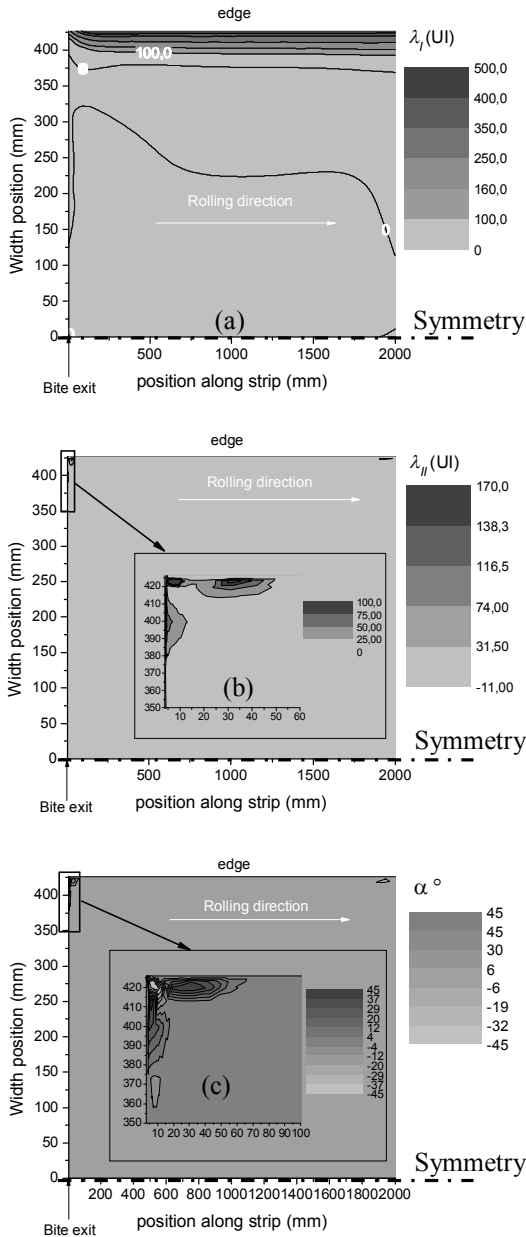


Figure 3: Flatness defect prediction. a : first principal buckling strain λ_I , b : second principal buckling strain λ_{II} , c : angle α defining the eigendirections of the buckling strain λ .

The basic idea of the ANM consists in searching the solution path of the non-linear problem (2) under an asymptotic expansion form with respect to a control parameter 'a'. This expansion is developed in the neighbourhood of a known regular solution (U_0, λ_0) as following:

$$\begin{aligned} U(a) &= U_0 + aU_1 + a^2U_2 \dots + a^nU_n \\ g(a) &= g_0 + ag_1 + a^2g_2 \dots + a^ng_n \\ a &= \langle u - u_0, u_1 \rangle + (g - g_0)g_1 \end{aligned} \quad (3)$$

Where $U = \begin{pmatrix} u \\ \tilde{\gamma} \\ S \end{pmatrix}$ and n is the truncation order of series.

Equation (2) can be written in the following simple form:

$$R(U, \lambda) = L(U) + Q(U, U) - gF = 0 \quad (4)$$

where $L(\cdot)$ is a linear operator, $Q(\cdot, \cdot)$ a quadratic one, F the external load vector and R the residual vector. If we substitute (3) in (4) and equating coefficients of the same power of a , the non-linear problem (4) will be transformed into a sequence of linear problems as follows:

order 1:

$$\begin{aligned} L_t^0(U_1) &= g_1F \\ \langle u_1, u_1 \rangle + g_1^2 &= 1 \end{aligned} \quad (5)$$

order p ($1 < p < n$):

$$\begin{aligned} L_t^0(U_p) &= g_pF - \sum_{r=1}^{p-1} Q(U_r, U_{p-r}) \\ \langle u_p, u_1 \rangle + g_pg_1 &= 0 \end{aligned} \quad (6)$$

$L_t^0(\cdot)$ is the tangent operator which depends only on the initial solution.

2.2.2 Applications and results

Several buckling academic applications and strip rolling cases had been analysed using ANM shell element model. Therefore, critical load (g_c) analytical evolutions with length/width ratio for free and simply supported edge cases where pure compression is considered (cf. [11]) are reproduced (cf. figure 4). Besides, for "case 1" (presented on table 1) out of bite stress fields become closer to experiments after buckling as mentioned in figure 5. Furthermore, figure 6 illustrates the rolled strip post-buckling state presenting wavy edges and longitudinal stationary waves near the bite exit. Moreover, we deduce correlation between the presented approaches in spite of their large differences.

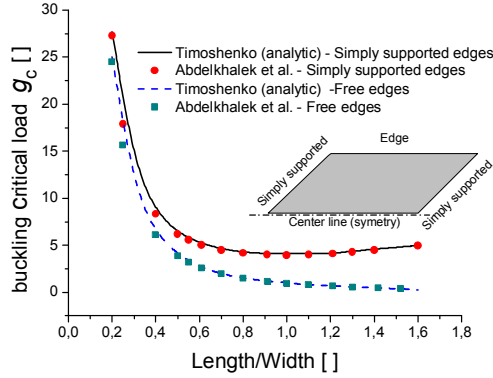


Figure 4: Critical load (g_c) evolution with length/width ratio for pure longitudinal compressive stress (-1 MPa) where simply supported and free edges are considered.

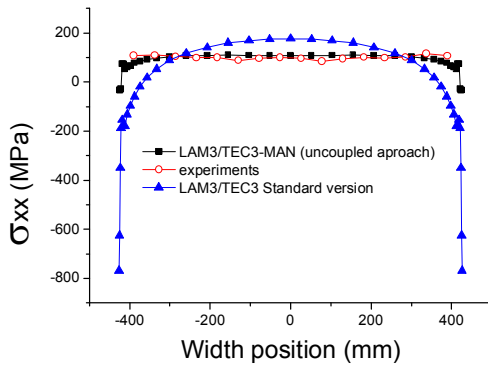


Figure 5: Comparison of longitudinal stress profiles computed with Lam3/Tec3 standard version and the uncoupled approach (Lam3/Tec3-MAN), and measured in experiments (far away enough from the bite).

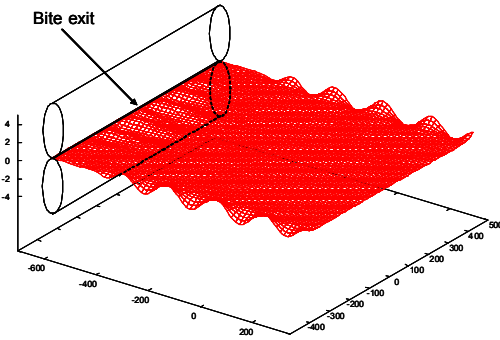


Figure 6: Flatness defect of rolled strip for case presented on table 1: wavy edges and longitudinal stationary waves near to the bite exit.

3 CONCLUSIONS

The flat product rolling – specialized FEM software Lam3/Tec3 has been complemented with a simple buckling model inspired by [3]. The computed stress profiles are therefore in very good agreement with experiments and the most important result at this stage is the weak influence of buckling on in-bite stress and strain fields. This was not expected, as out-of-bite relaxed stresses may be viewed as boundary conditions for the bite; but it provides a more

rigorous justification of the traditional decoupled methods of the literature using shell elements looked more adapted models for buckling. Here, decoupled method is adopted using Asymptotic Numerical Method (ANM) for shell element model which gives excellent buckling computing capability with more realistic results. Thus it looks much more precise and predictive buckling model, in particular allowing modelling of post-buckling.

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